### 2. Algebraic expressions, equations, inequalities

# Task 2.1. (T 16.2015, 0 - 4 pts)

Write down each of the following as an algebraic expression.

- a) the cube of the sum of a and b.

### Task 2.2. (T 4.2016)

If  $m = \frac{1-x^2}{x+1}$ , n = x - 1, where  $x \neq -1$  then the difference between m and n equals

**A.** 0

**B.** 2-2x **C.** -2x

**D.**  $\frac{-x^2-x+2}{x+1}$ 

### Task 2.3. (T 19.2016, 0 – 2 pts)

The equation  $mx^2 + 2x - 1 = 0$  is solved for x. Complete the following sentences.

- a) If m = -1, then the number of solutions to this equation is ......
- b) If the number  $x_0 = \frac{1}{2}$  is the solution to this equation then  $m = \dots$

## Task 2.4. (T 3.2017)

If m = 5 and n = 4, then the difference of squares of m and n is:

**A.** 41

**B.** 1

**C.** 81

**D.** 9

#### Task 2.5. (T 4.2017)

 $\begin{cases} 2x + y = 3 \\ 4x - 5y = -1 \end{cases}$  is a system of equations which is represented in two-dimensional system of coordinates by:

A. an infinite set

- В. an empty set.
- C. exactly two distinct points.
- D. exactly one point.

### Task 2.6. (T 5. 2017)

The sum of all roots of the equation (x - 3)(x - 2)(x + 6) = 0 is:

- **A.** -1
- **B.** 1
- **C.** −11
- **D.** 11

### Task 2.7. (T 11.2018)

The set of all real numbers x which satisfy the inequality: -3 < 2x - 1 < 3 is

- **A.** (-3;3) **B.** (-3;3) **C.** (-1;2) **D.** (-1;2)

## Task 2.8. (T 2.2019)

For each real number *x* and for each real number *y* the square of the difference  $(x^2 - 5y)^2$  equals:

A.  $x^4 - 10x^2y + 25y^2$ 

B.  $-x^4 + 10x^2y - 25y^2$ 

C.  $x^4 + 25y^2$ 

**D.**  $x^4 - 25y^2$ 

## Task 2.9 (T 3.2019)

The set of simultaneous equations  $\begin{cases} 3x + 5y = -1 \\ x - 11y = 6 \end{cases}$  in a set of coordinate axes:

A. describes an infinite set.

- **B.** describes an empty set.
- **C.** describes exactly two distinct points.
- **D.** describes exactly one point.

#### Task 2.10 (T 2.2020)

The product of all solutions of the equation (x-1)(x+2)(x-3) = 0 is:

- **A.** −6
- **B.** -2
- **C.** 2
- **D.** 6

# Task 2.11 (T 3.2020)

If x + y = 25 and x - y = -4, then  $x^2 - y^2$  equals:

- **A.** -100
- **B.** −29
- **C.** 29
- **D.** 100

# Task 2.12. (T 8.2020)

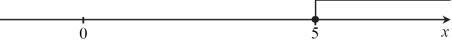
The expression 2(x-3) - 5x(3-x) can be written as:

- **A.** -10x(x-3) **B.** 10x(x-3)
- **C.** (5x-2)(x-3) **D.** (5x+2)(x-3)

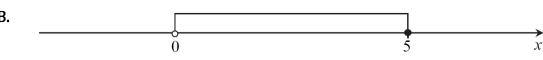
# Task 2.13. (T 9.2020)

The solution set for the inequality  $2 - \frac{2}{3}(x-1) \ge -\frac{2}{3}$  is the interval:

A.



B.



C.

D.



### Task 2.14 (T 18.2020, 0 – 2 pts)

The geometrical interpretation of the set of simultaneous equations

$$\begin{cases} x + y = 2 \\ x + (1+m)y = 1 \end{cases}$$

with the unknowns x and y are:

- a) two parallel lines, when *m* equals ......
- b) two perpendicular lines, when *m* equals ......

### Task 2.15 (T 1.2021)

The square of the difference of 3x and y, minus the square of the sum of x and 3y is

**A.** 
$$8x^2 + 8y^2 - 12xy$$

**B.** 
$$8x^2 - 8y^2$$

**C.** 
$$8x^2 - 8y^2 - 12xy$$
 **D.**  $8x^2 + 8y^2$ 

**D**. 
$$8x^2 + 8y^2$$

#### Task 2.16 (T 3.2021)

The solution for the inequality

$$\frac{x-2}{2} - \frac{9-x}{3} > \frac{1}{6}x - 10$$

is

**A.** 
$$(-9; +\infty)$$

**A.** 
$$(-9; +\infty)$$
 **B.**  $\left(-\frac{36}{11}; +\infty\right)$  **C.**  $\left(\frac{7}{2}; +\infty\right)$ 

C. 
$$\left(\frac{7}{2}; +\infty\right)$$

# Task 2.17. (T 4.2021)

The greatest real root of the equation x(x + 1)(3x + 4) = 0 is

- **B.** 0
- **C.** 2
- D.  $-\frac{4}{3}$

#### Task 2.18 (T 3.2023)

Complete the sentence. Select the correct answer from the options given below.

The number of all real solutions of the equation  $x(x^2 + 1)(x - 2) = 0$  is

- **A.** 1
- B. 2
- **C.** 3
- **D**. 4

## Task 2.19 (T 4.2025)

The numbers  $x = 5 - 2\sqrt{2}$  and  $y = 2 - 5\sqrt{2}$  are given.

Complete the sentence. Choose the correct answer from the options given below.

The absolute value of the difference of the squares of the numbers x and y is equal to

- **A.** 21
- **B.**  $79 + 40\sqrt{2}$
- **C.** 63
- **D.**  $21 + 40\sqrt{2}$

### Task 2.20 (T 5.2025)

One of the solutions of the equation  $x \cdot (x^2 - 4x + m) = 0$  with the unknown x is the number 2.

Complete the sentence. Choose the correct answer from the options given below.

The number m is equal to

- **A.** -4
- **B.** -2
- **C.** 2
- **D.** 4